

# Using Planck Clusters for Cosmology and Calibration

Subha Majumdar

Tata Institute of Fundamental Research, Mumbai

# What can we do with Planck clusters ?

There are so many ways to do cosmology with clusters that we are spoilt with choice (*but unfortunately NOT with numbers in SZ*):

**Cluster counts**

**SZ power spectrum**

**Use clusters as rulers**

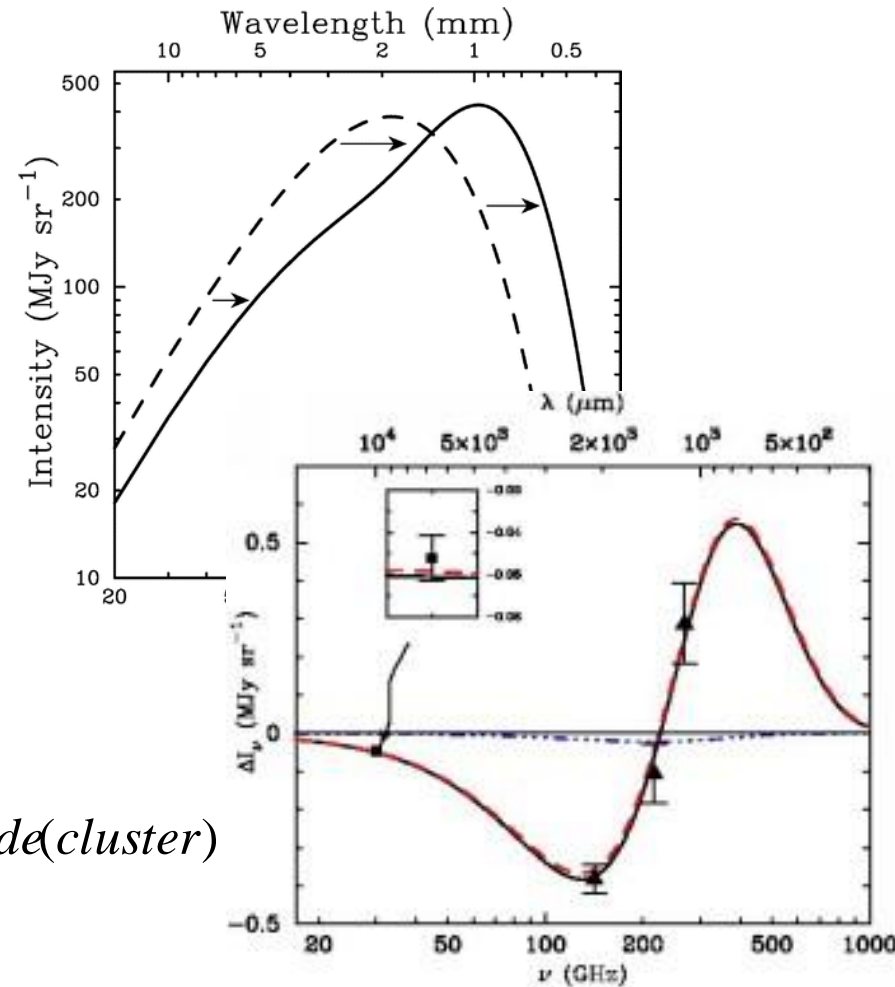
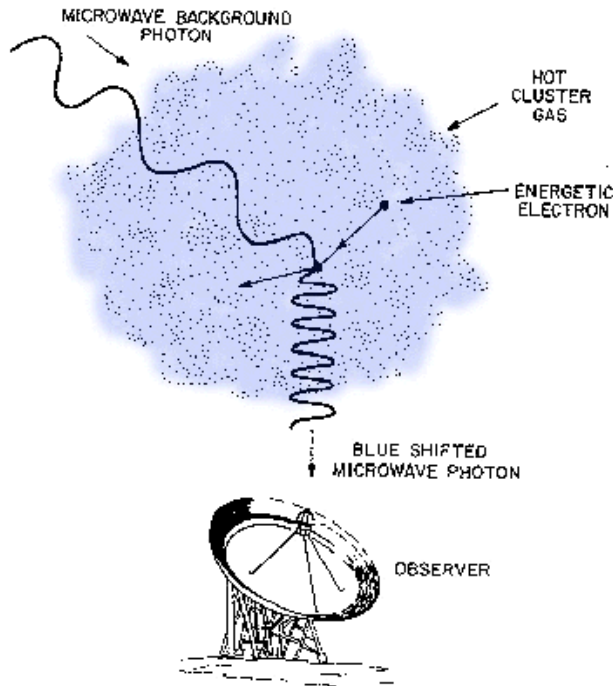
2D/3D  $P(k)$

Cluster gas fraction

Mass/Luminosity function

**Calibration sample within Planck or other cluster surveys**

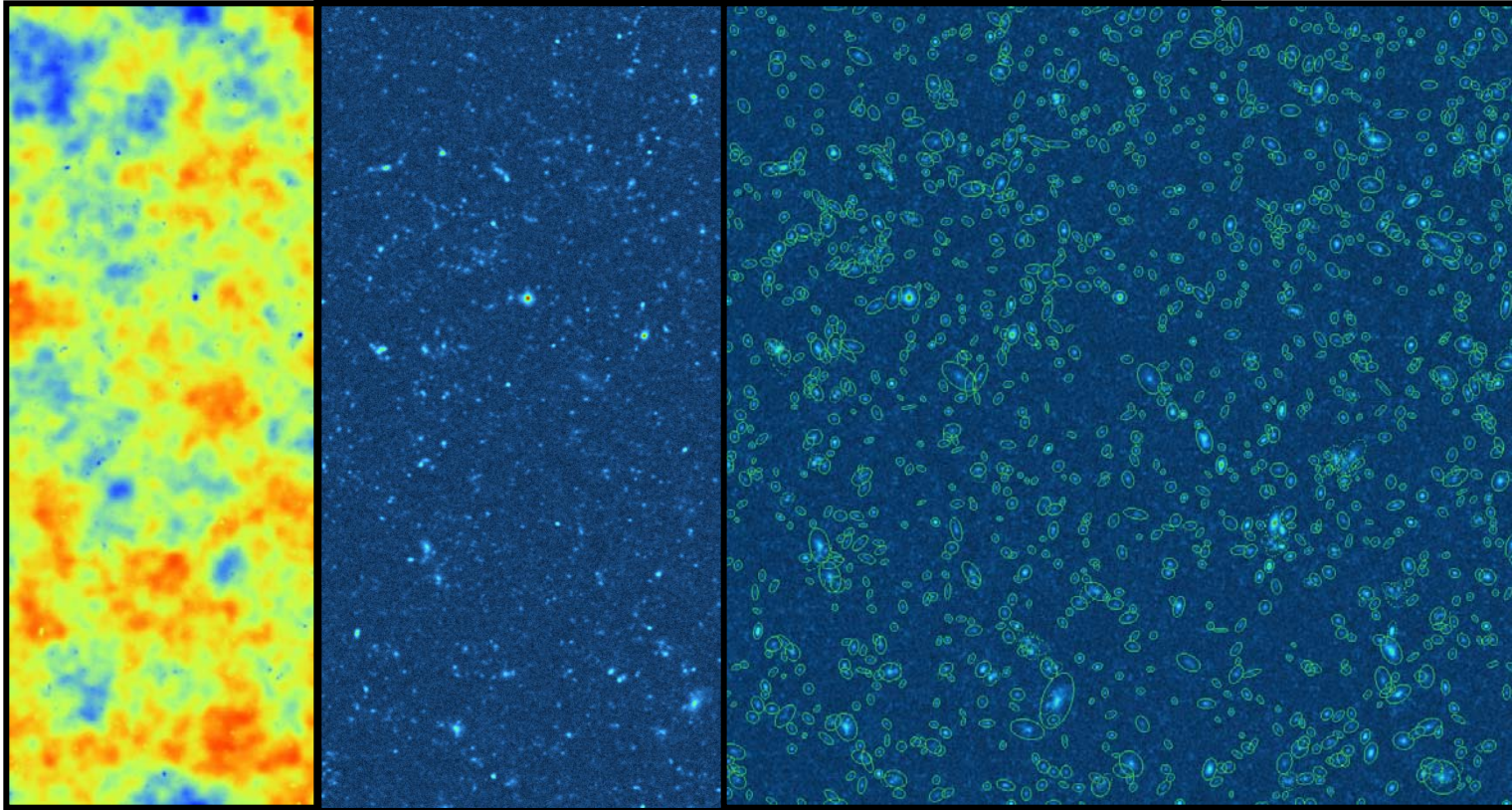
# The basics of SZ Effect...



$distortion = freq\_dependence \times amplitude(cluster)$

$amplitude \propto \int_{line-of-sight} gas\_pressure$

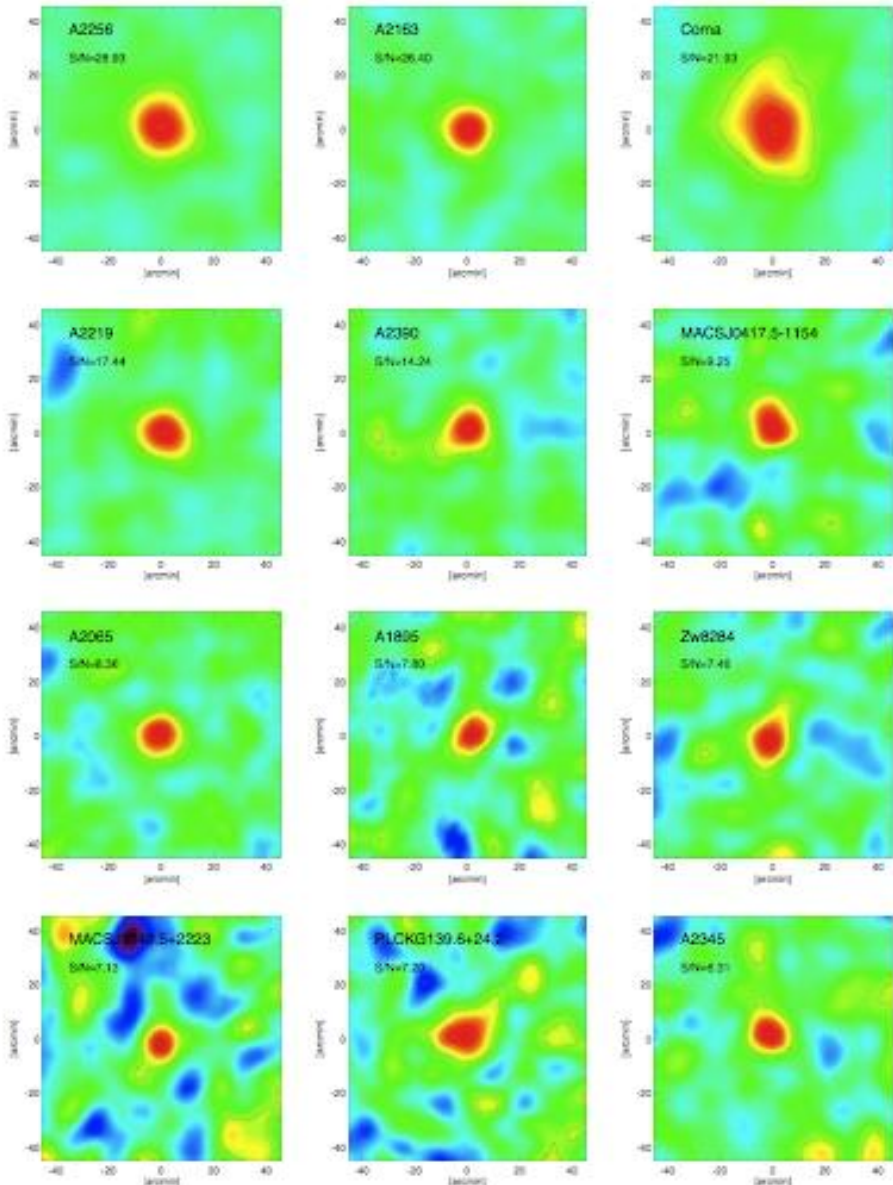
# SZ clusters in Planck



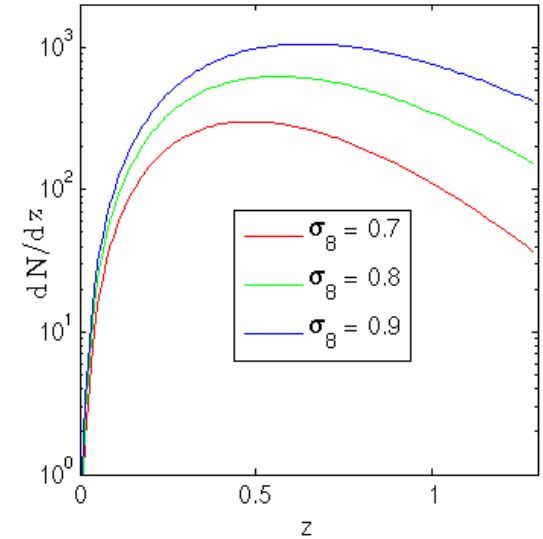
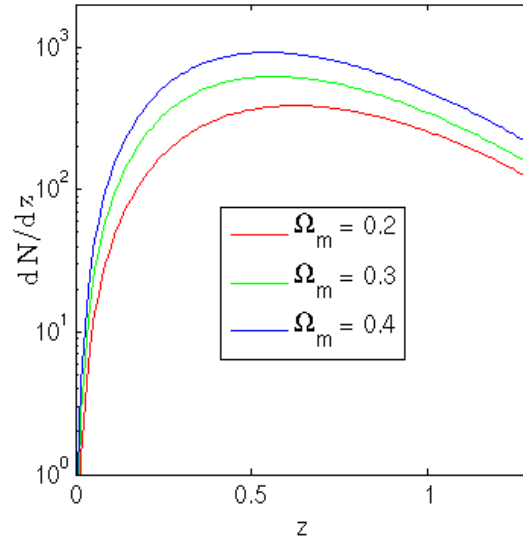
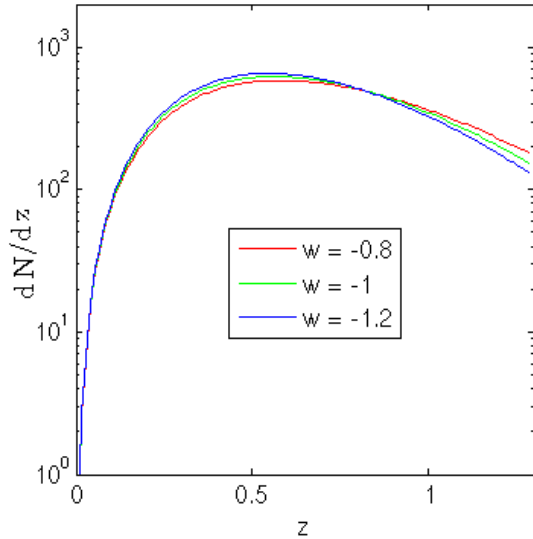
$10^\circ \times 10^\circ$  map  
145 GHz

Diego & SM

# Planck clusters *circa* Jan 2011



# Cosmology with cluster numbers ?

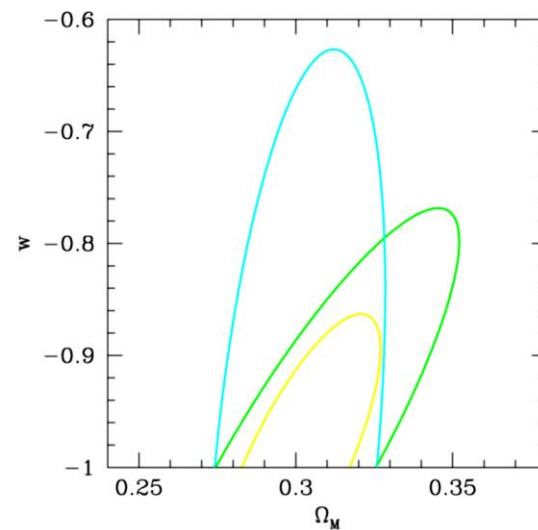
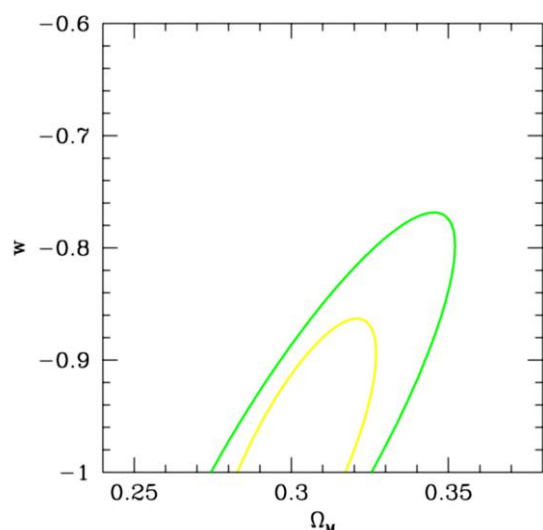
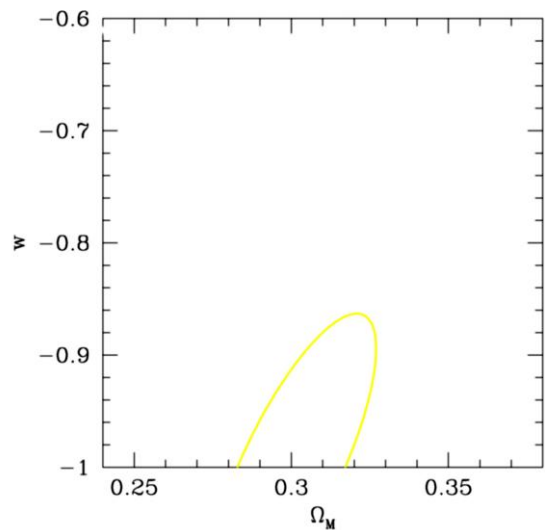
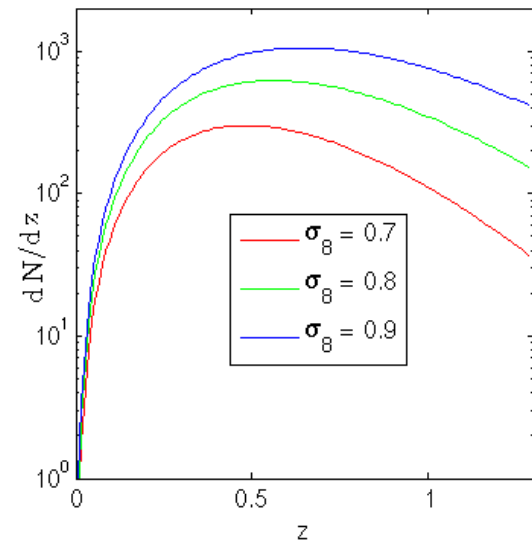
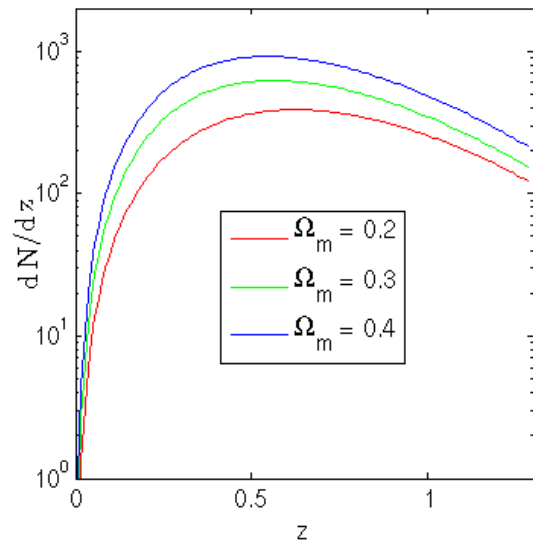
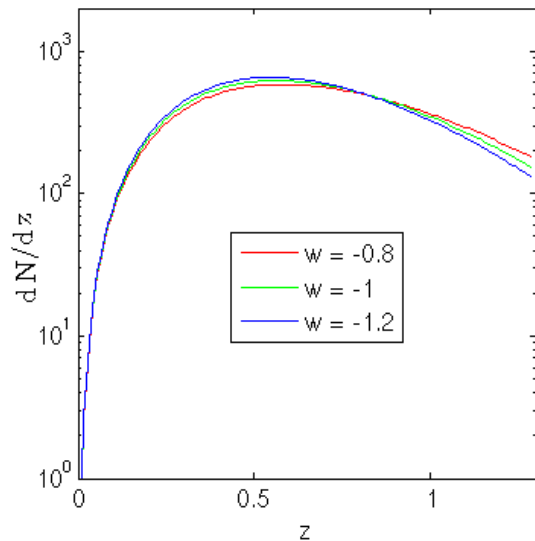


$$N(>z) = \int_{z_{\min}}^{z_{\max}} dz \frac{dV}{dz} \int_{M_{\min}}^{M_{\max}} dM \frac{dn(M, z)}{dM} F(M|z, O, sc, N, \dots)$$

For the diffuse sky:

$$C_l = g_v^2 \int_{z_{\min}}^{z_{\max}} dz \frac{dV}{dz} \int_{M_{\min}}^{M_{\max}} dM \frac{dn(M, z)}{dM} |y_l(M, z)|^2$$

# Cosmology with cluster numbers ?



Only cosmology  
 $F(M|...) = 1$

Uncertain  $F(M|O..)$  locally

Also need to know  
 $z$  behaviour of  $F$

# The 'really' big question...

## How many clusters will Planck find?

**Good news:** First set of Planck papers already has cluster catalog. Planck is indeed giving us an SZ selected all sky cluster catalog. Companion Planck papers have studied the cluster properties in details. Followup observations have also been done. Cross calibration with optical and Xrays done.

**Bad News :** We hoped for much larger sample!

Bartelmann 2001 :  $N \sim \text{few times } 1e4$

Moscardini etal 2002 :  $M_{\text{lim}} \sim 3.2/h e14$  for  $z > 0.2$

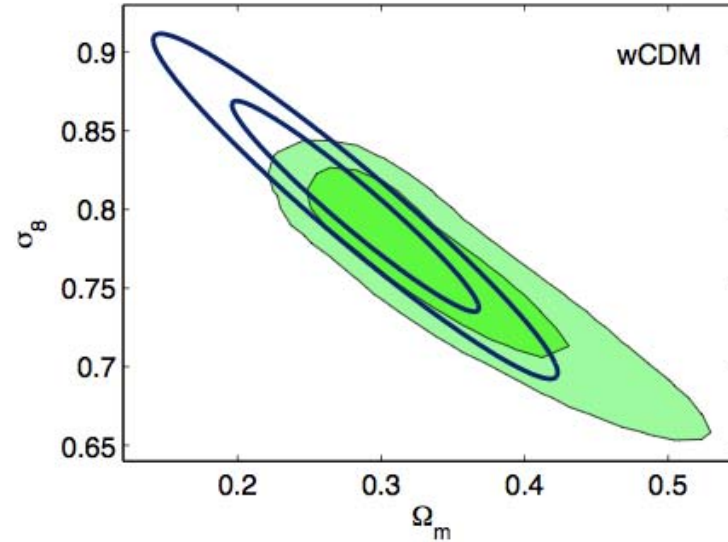
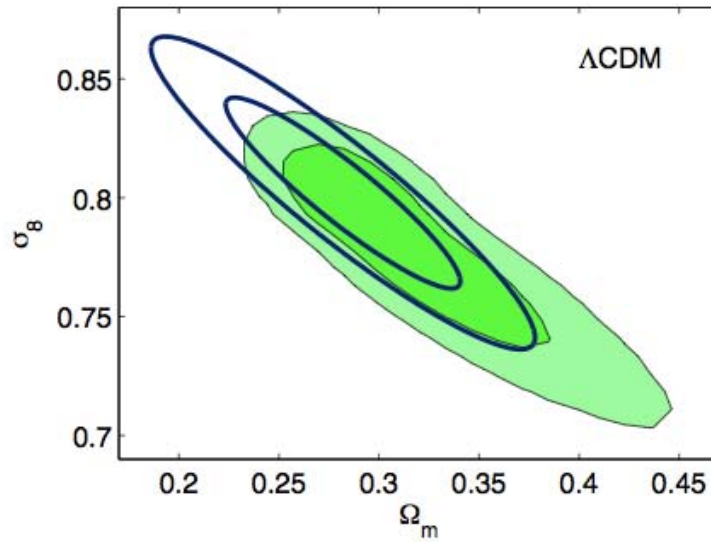
Schaeffer & Bartelmann 2007:  $M > 2.5/h e14 M_{\text{sun}}$  between  $0.2 < z < 0.8$

SM & Mohr 2004 :  $N \sim 20000$

**Reality :**  $N \sim 1000-2000$ ,  $M_{\text{lim}} \sim 8e14/h M_{\text{sun}}$

# Expectations (with external mass calibration) ...

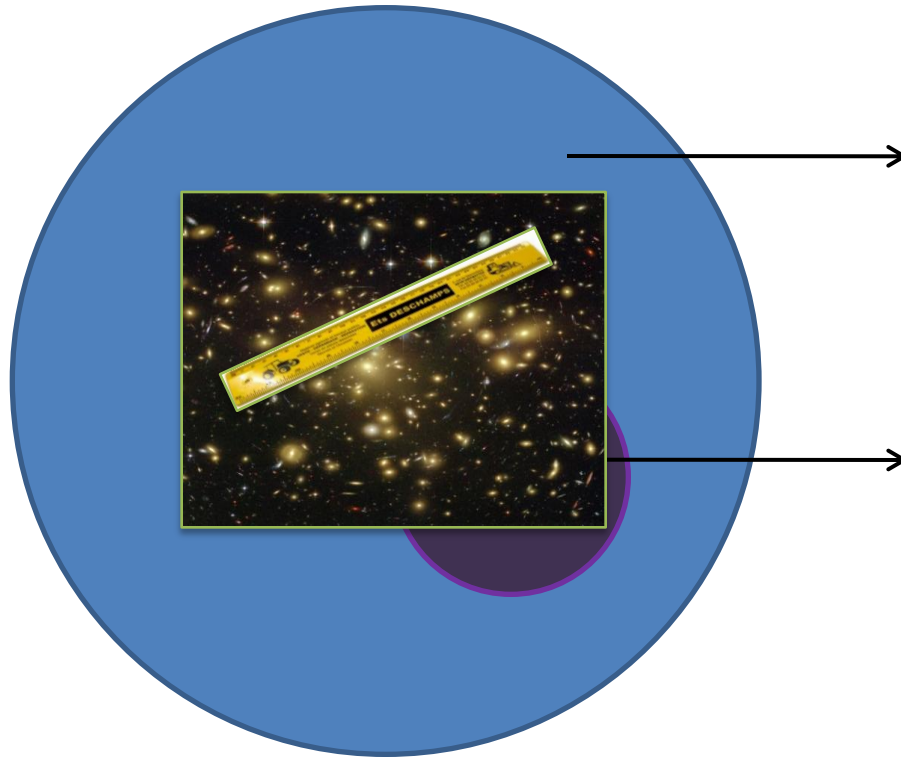
Khedekar & SM, 2011



model parameter	Planck			
	$\Lambda$ CDM		$w$ CDM	
	MCMC	Fisher	MCMC	Fisher
$\Omega_m$	0.044	0.039	0.064	0.057
$w_0$	—	—	0.199	0.189
$\sigma_8$	0.028	0.026	0.041	0.044
$A$	1.453	1.222	1.581	1.423
$\alpha$	0.098	0.082	0.107	0.096
$\gamma$	0.136	0.146	0.184	0.181

0.01  
0.175  
0.056

# Once eROSITA is launched ...



## XRAY SURVEY

*eROSITA ~ all sky.  
(Maybe XMM at present)*

## SZ SURVEY

*Planck ~ all sky  
(also SPT/ACT ~ 2 k sq.  
deg.)*

**Find common clusters in the region of overlap between the 2 surveys.**

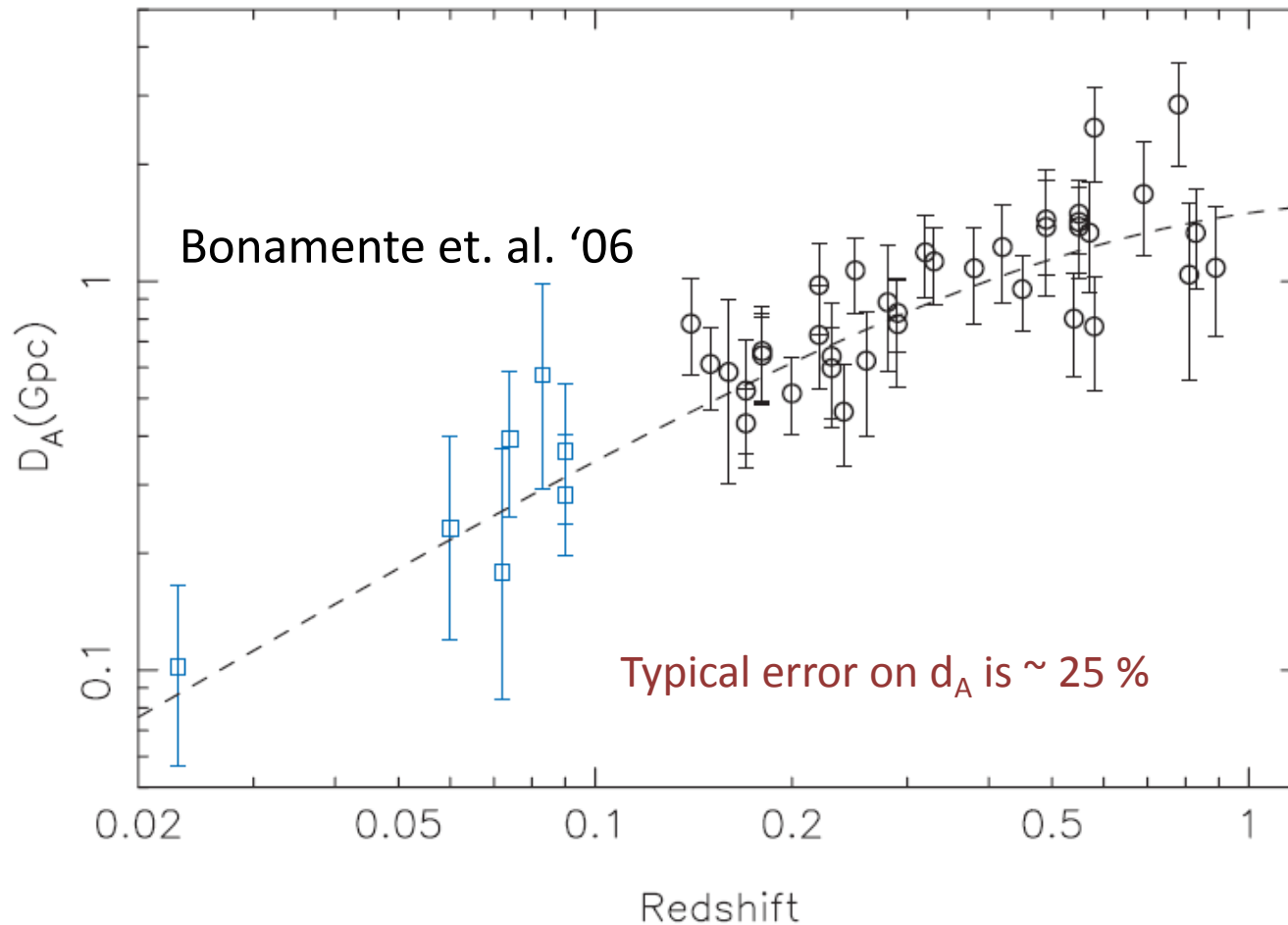
Common clusters also ideal for Xray mass calibration (since Y-M can be compared)

--> so  $\langle T \rangle$  should target these.

SZ clusters will have first go at the z's.

***ESTIMATE  $d_A(z)$  for each cluster.***

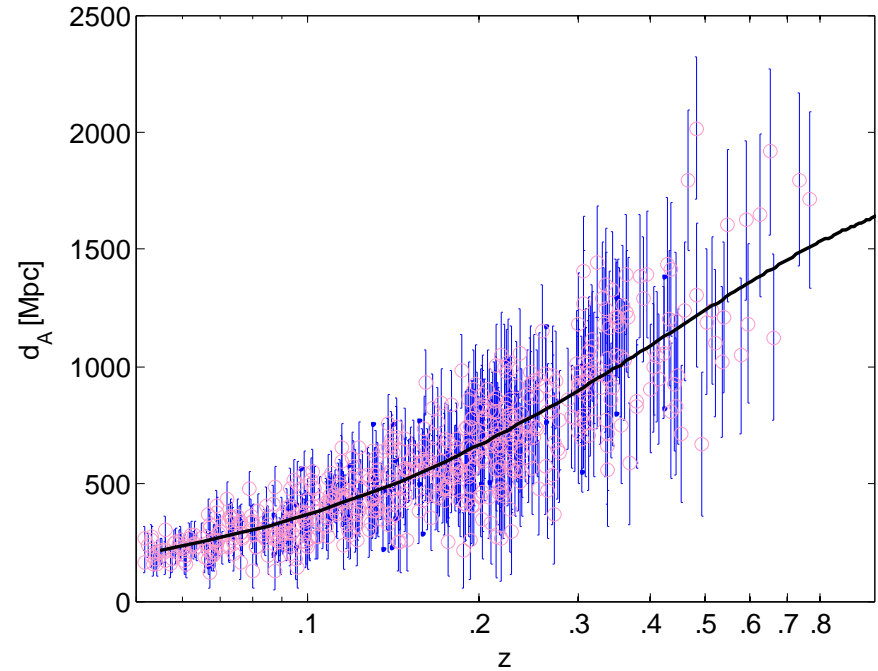
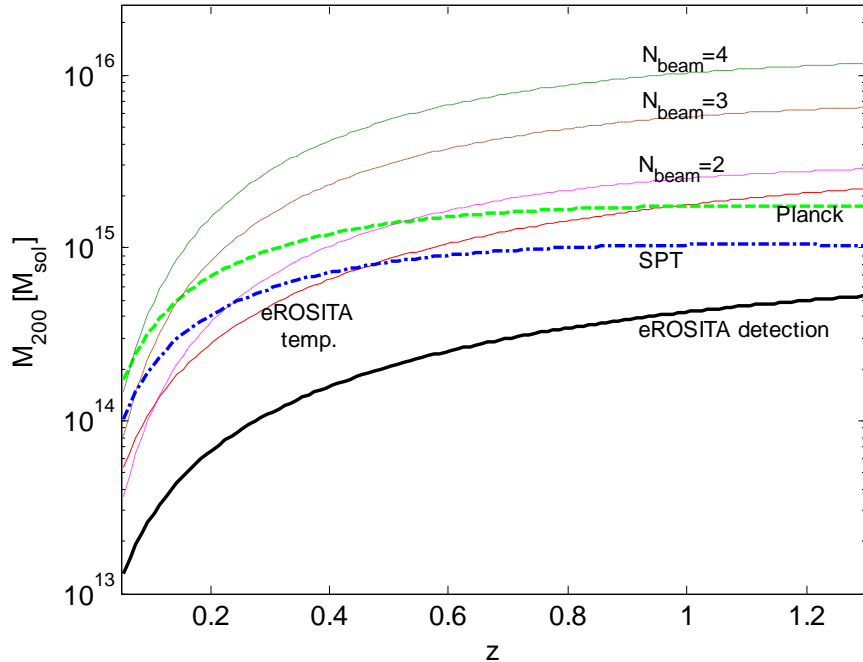
# Current data on dA...



38 clusters  
Chandra  
+ OVRO  
+ BIMA

Also Reese et. al. in '02

# Xray+SZ survey synergy - making a mock $d_A(z)$ ...



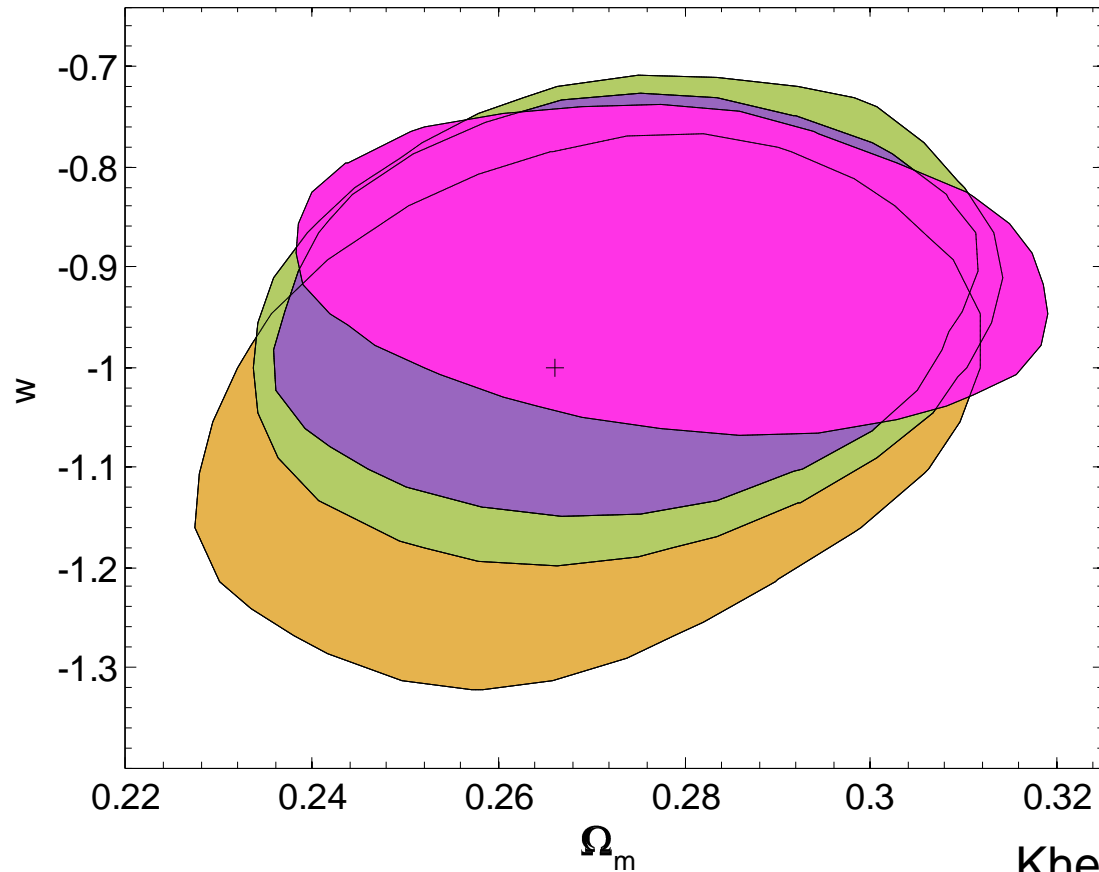
$$\theta_c \geq N_{\text{beam}} \theta_{\text{fwhm}};$$

$$\theta_{\text{fwhm}} = 16'' \text{ for eROSITA}$$

mock catalog of  $d_A$  created from **SZ + eROSITA** for  $N_{\text{beam}}=2$  with **25% errors (and scatter)** in  $d_A(z)$ .

# Planck(dN/dz) + overlap with eROSITA

*effect of various datasets...  $N_{beam}=2, 3, 4$*



Khedekar & SM 2010

# Something different ...

For the next few slides we'll leave Planck and go to Xray survey and use Planck cluster data as calibrator.

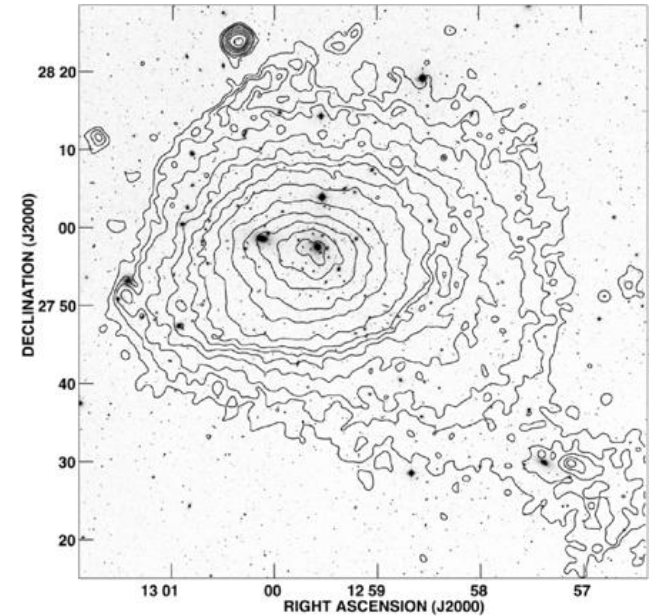
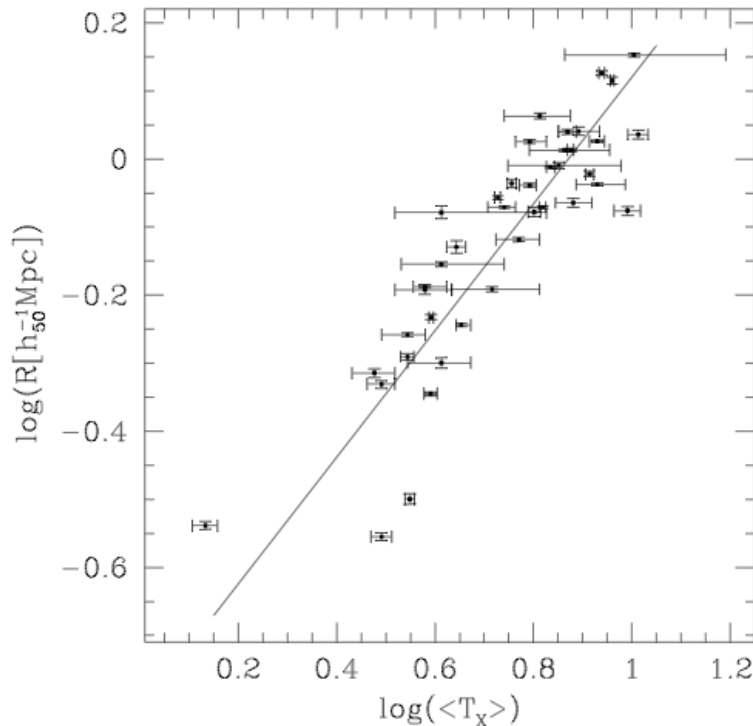
Something for the future: **The Wide Field Xray Telescope**  
(PI - Riccardo Giacconi)

# Xray Isophotes and scalings...

$$I(R) = A\Lambda\rho_0^2 R_c [1 + (R/R_c)^2]^{-3\beta+1/2}$$

$$f_{ICM} = \frac{4\pi\rho_0 R_c^3 \int_0^{R_{vir}/R_c} d\lambda \lambda^2 (1 + \lambda^2)^{-3\beta/2}}{M_{vir}}$$

$$I(R) = C f_{ICM}^2 R^{-6\beta+1}$$



$$R_I = \sqrt{A_I/\pi}$$

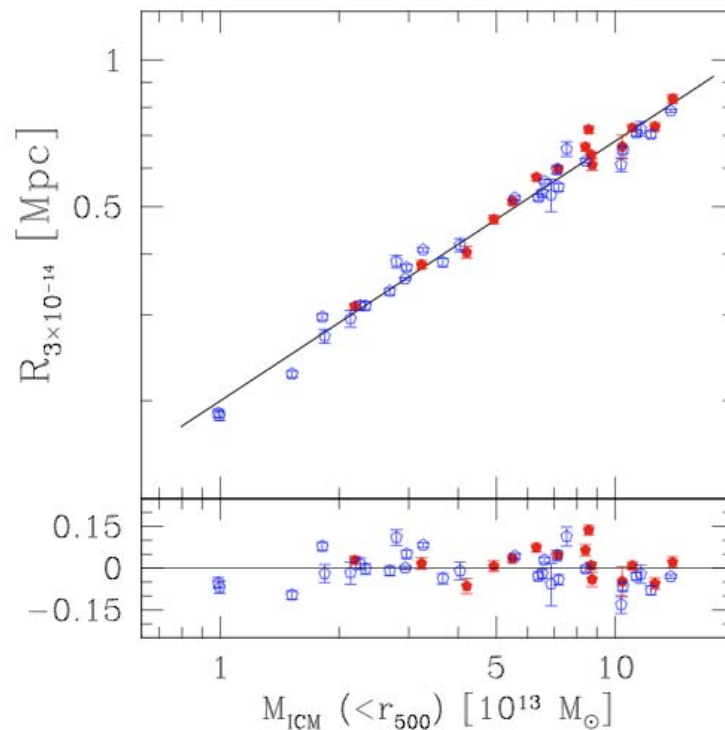
$$\log R_I = (0.93 \pm 0.11) \log \frac{\langle T_X \rangle}{6 \text{ keV}} - (0.08 \pm 0.01)$$

AN X-RAY SIZE-TEMPERATURE RELATION FOR GALAXY CLUSTERS:  
OBSERVATION AND SIMULATION

JOSEPH J. MOHR<sup>1,2</sup> & AUGUST E. EVRARD<sup>1,3</sup>

# A very low scatter scaling ...

Scaling Relation	Simulations <sup>a</sup>	
	Original Relations	$\sigma_{\text{int}}$
$M_{\text{ICM}}(<r_{500})-T_X$	0.17	0.20
$M_{\text{ICM}}(<r_{2500})-T_X$	0.22	
$L_X(<r_{500})-T_X$	0.53	
$L_X(<r_{2500})-T_X$	0.67	
$L_{\text{XCS}}(<r_{500})-T_X$	0.28	0.27
$R_{3 \times 10^{-14}}-T_X$	0.14	0.10
$R_{1.5 \times 10^{-13}}-T_X$	0.17	
$L_{\text{NIR}}(<r_{500})-T_X$	0.19	
$R_{3 \times 10^{-14}}-M_{\text{ICM}}(<r_{500})$	0.06	
$R_{3 \times 10^{-14}}-L_{\text{XCS}}(<r_{500})$	0.05	
$R_{3 \times 10^{-14}}-L_{\text{NIR}}(<r_{500})$	0.16	



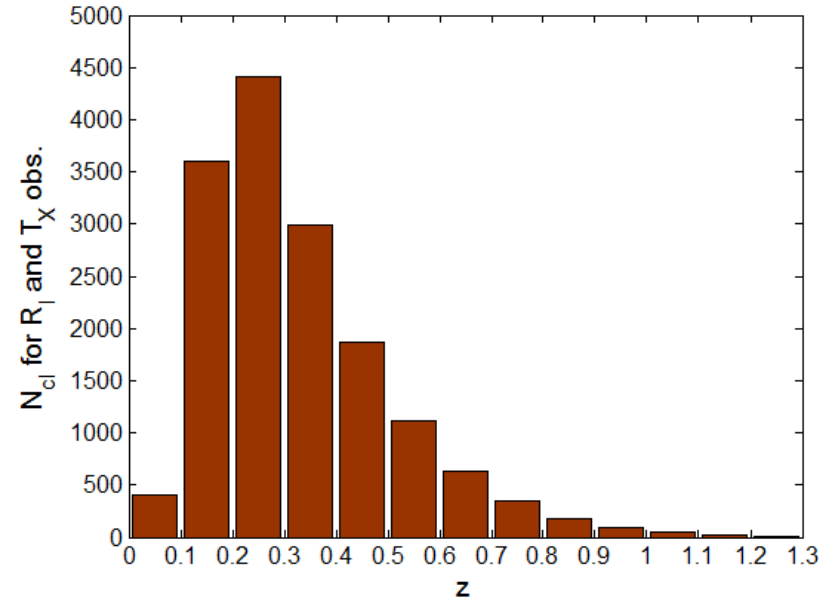
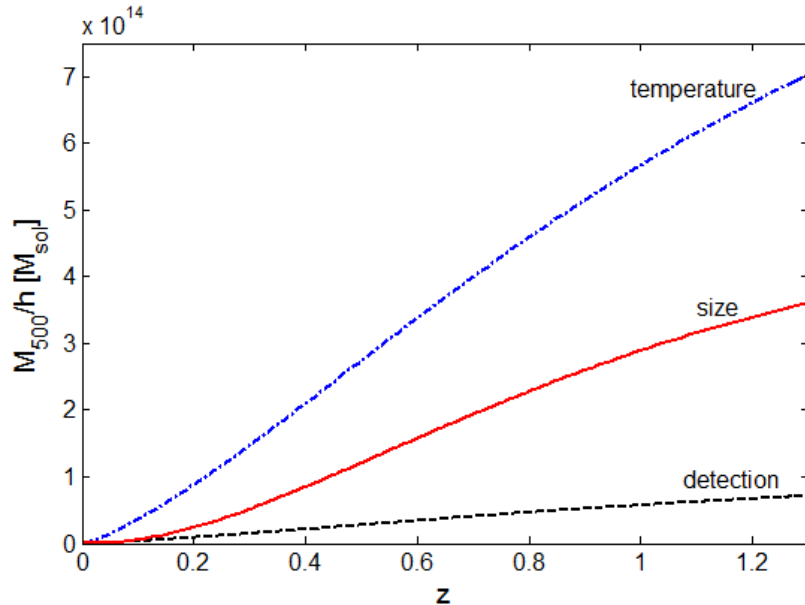
Compare this with ~10% scatter of  $Y_X$ - $M$  reln  
(with central region excised)

Given that  $M_{\text{gas}}-M_{\text{tot}}$  has  
very low scatter -->  
 $R_I-M_{\text{tot}}$  very low scatter.

*(O'Hara et al 2006)*

# Constructing a mock catalog of WFXT isophotes .

Khedekar, SM & Mohr, 2011

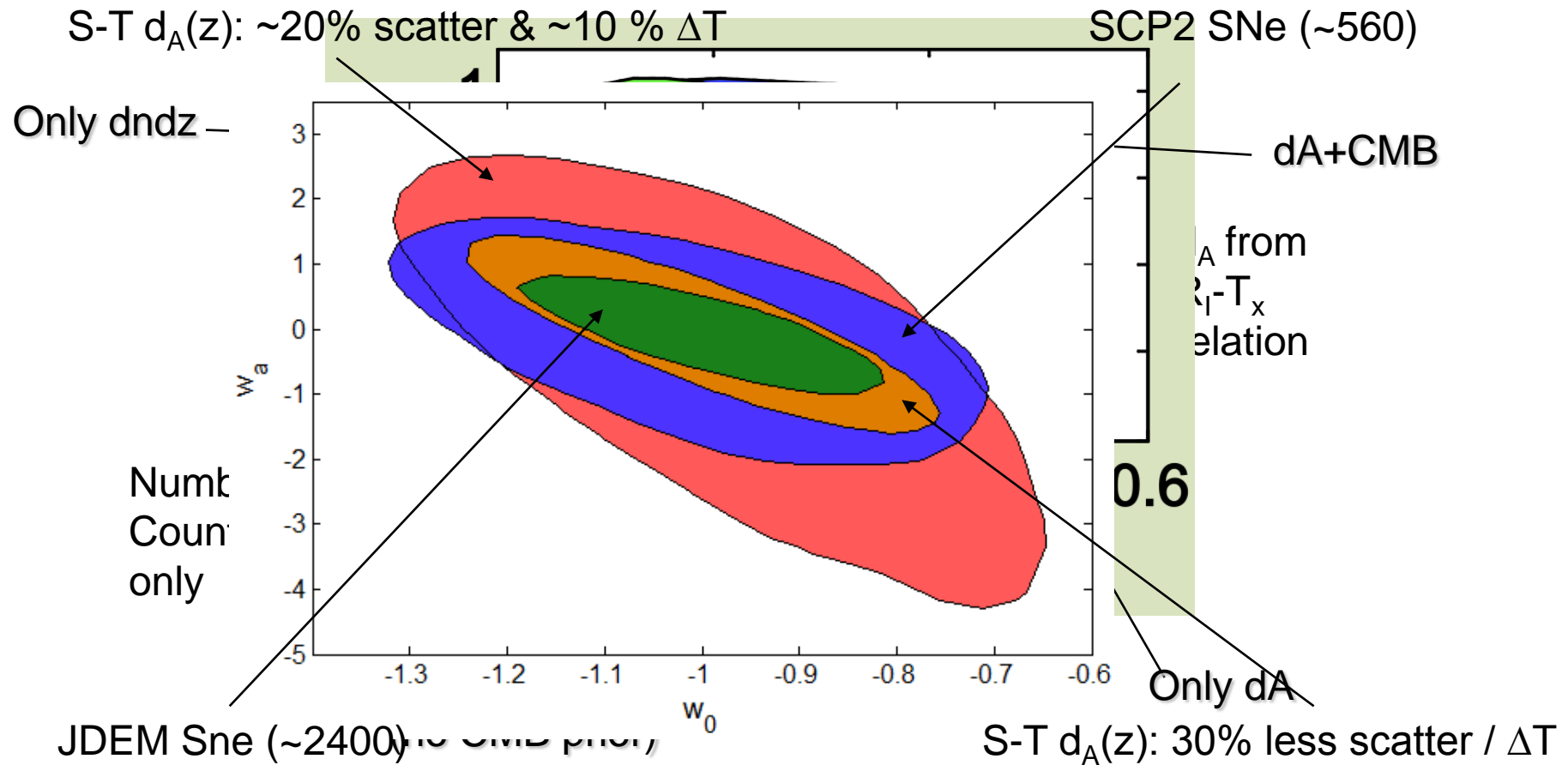


**~15,000 clusters** assuming a minimum of 2000 photon cts in [0.5-2.0 keV] band.

Isophotal sizes of all these clusters may be determined with a high precision ( $\theta_l \geq 10 \theta_{beam}$ ).

$$\frac{\Delta\theta_l}{\theta_l} = \frac{1}{2} \frac{\Delta A}{A} \simeq \frac{1}{\sqrt{2\pi}} \left( \frac{\theta_b}{\theta_l} \right)^{3/2} \sim 1\% \text{ error}$$

# First attempt at cosmology with size – temp from Xrays : Use Planck clusters as calibrators



Very conservative estimate - Unknown evolution is the killer as its completely degenerate with  $w(a)$  when distance is measured.

More about internal calibration with Planck SZ cluster sample

And connected to it - the SZ power spectrum.

But first: lets talk Universal features in clusters.

# Universal Profiles...

for isolated halos,  
e. **Based on GNFW**  
**model (Nagai etal)**

$$P_U \sim f(r_{500}, P_{500})$$

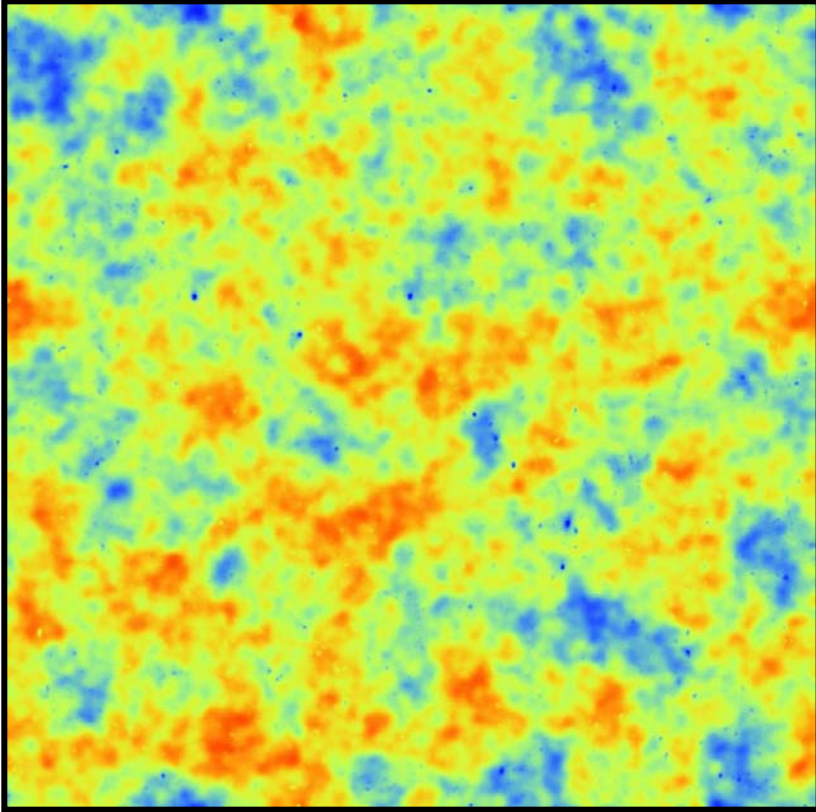
QuickTime™ and a  
TIFF (Uncompressed) decompressor  
are needed to see this picture.

gas do  $P_{500} \sim g(M_{500}, r_{500})$  not show universality.  
(I predicted it a year before) that

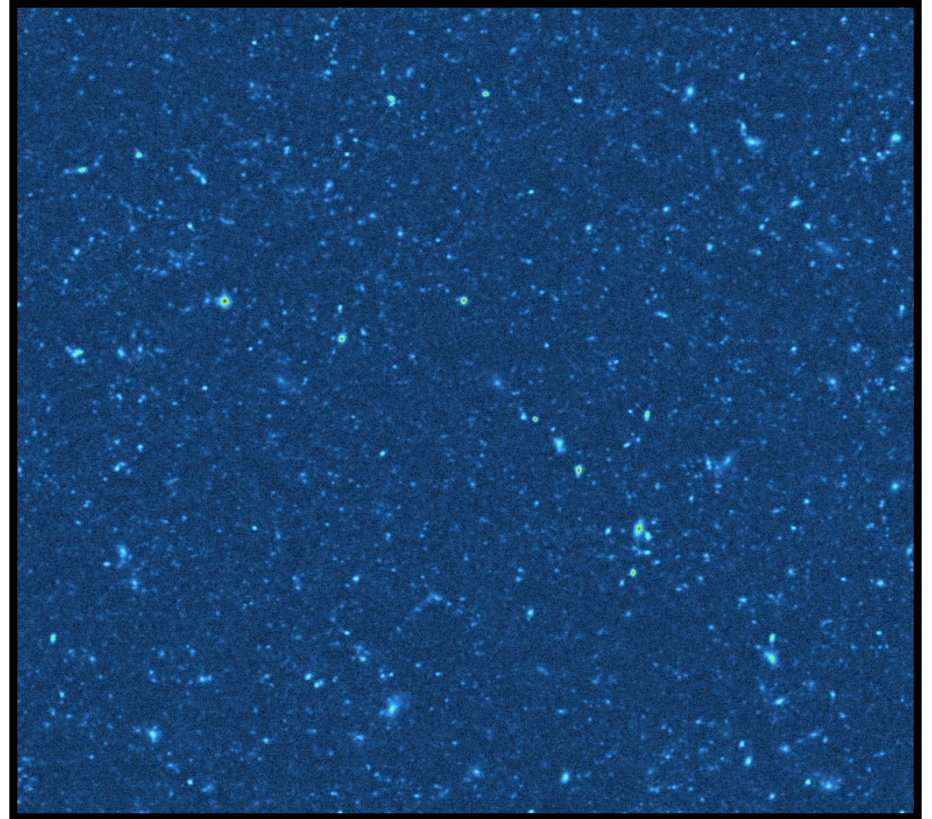
Arnaud etal 2010

All models now **'must'** reproduce this universal profile in **shape & amplitude** for any given cluster mass.

# Planck SZ power spectrum ..



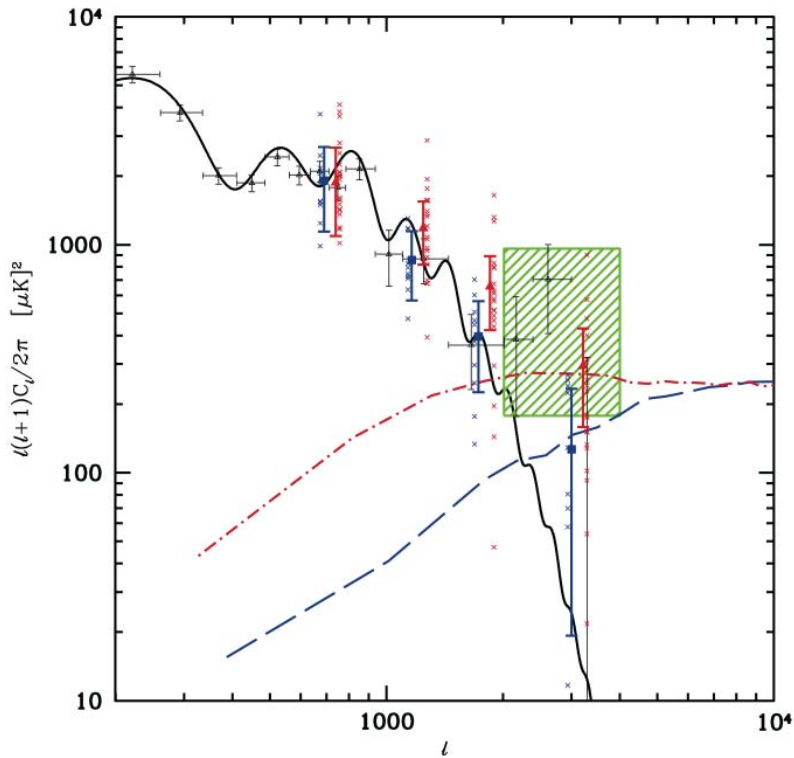
10° x 10° map  
145 GHz



Diego & SM

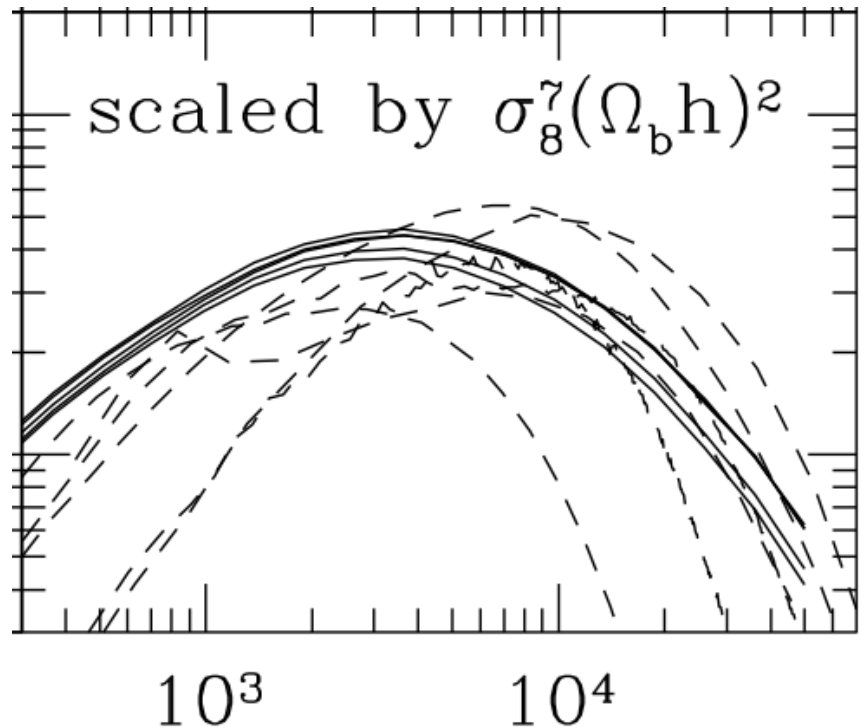
$$C_l = g_\nu^2 \int_{z_{\min}}^{z_{\max}} dz \frac{dV}{dz} \int_{M_{\min}}^{M_{\max}} dM \frac{dn(M, z)}{dM} |y_l(M, z)|^2$$

# More on SZ power spectrum - Importance of modelling



CBI observations  
(ask Carlo)

KS 2001



Comparison of analytic and simulation models *till 2009*.

**Factor of 2 offset in SZ power --> 0.1-0.15 offset in value of  $\sigma_8$  !**

Current (2011) agreement to SZ Cl's from different group  $\sim 20\%$ .

To be competitive with Planck CMB constraint in  $\sigma_8$  ( $\sim \Delta\sigma_8 = 0.01$ ), we need to know SZ Cl to  $< 10\%$  accuracy.

This is not easy to do in 'bottom up scenario'.

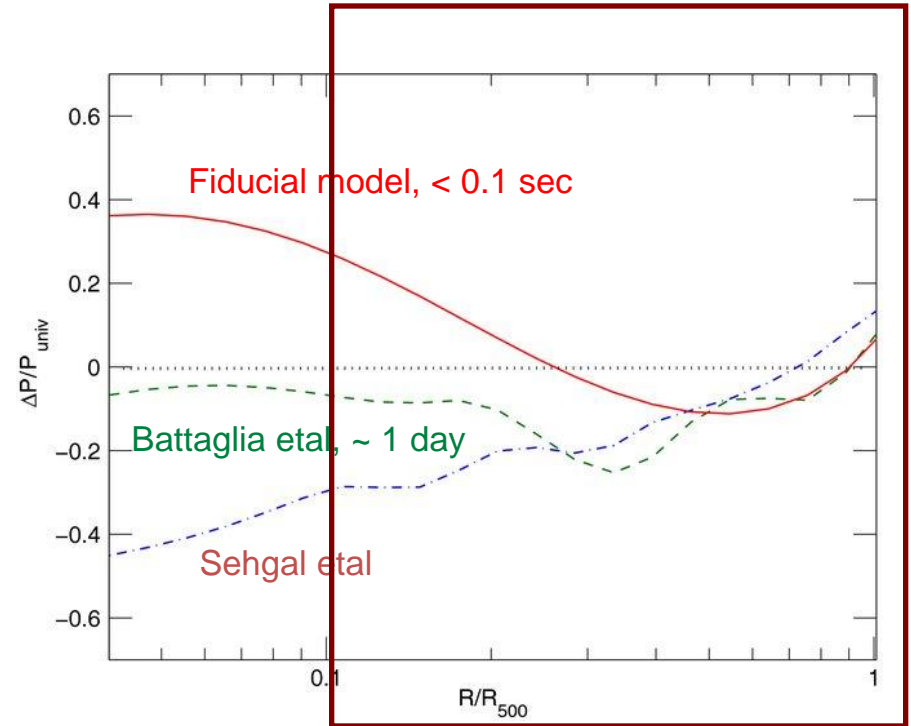
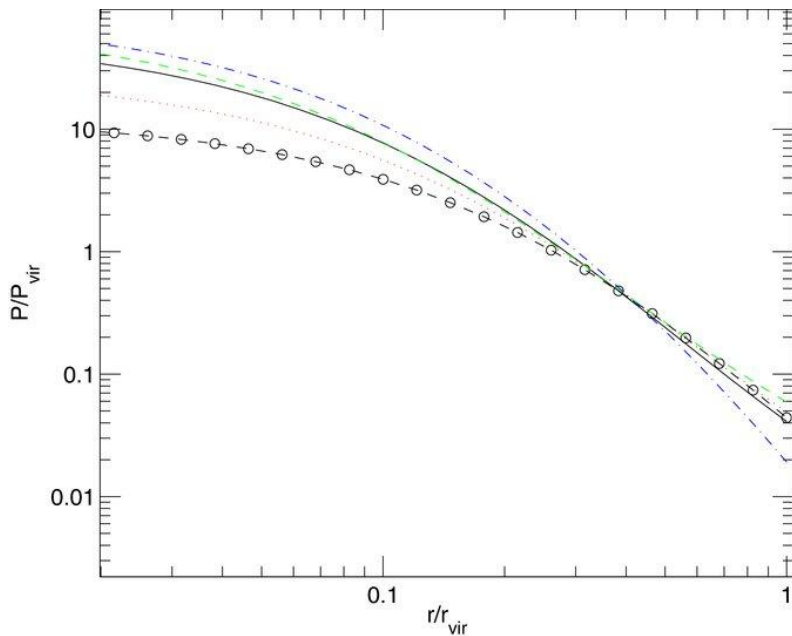
Ultimately, we want cluster 'pressure template' to be accurate to  $\sim 10-15\%$   
We also need to know how this template evolves with redshift.

----> First step- build a simple 'phenomenological models' and calibrate it to SZ cluster observations (especially from within Planck).  
The model also needs to be computationally fast.

**Note: We use Planck Y-T reln for calibration.**

# Pressure profile for the clusters -

A simple, semi-analytic, phenomenological, iterative model which uses known (say Xray scaling relns) as inputs for normalization along with a non-thermal pressure component.



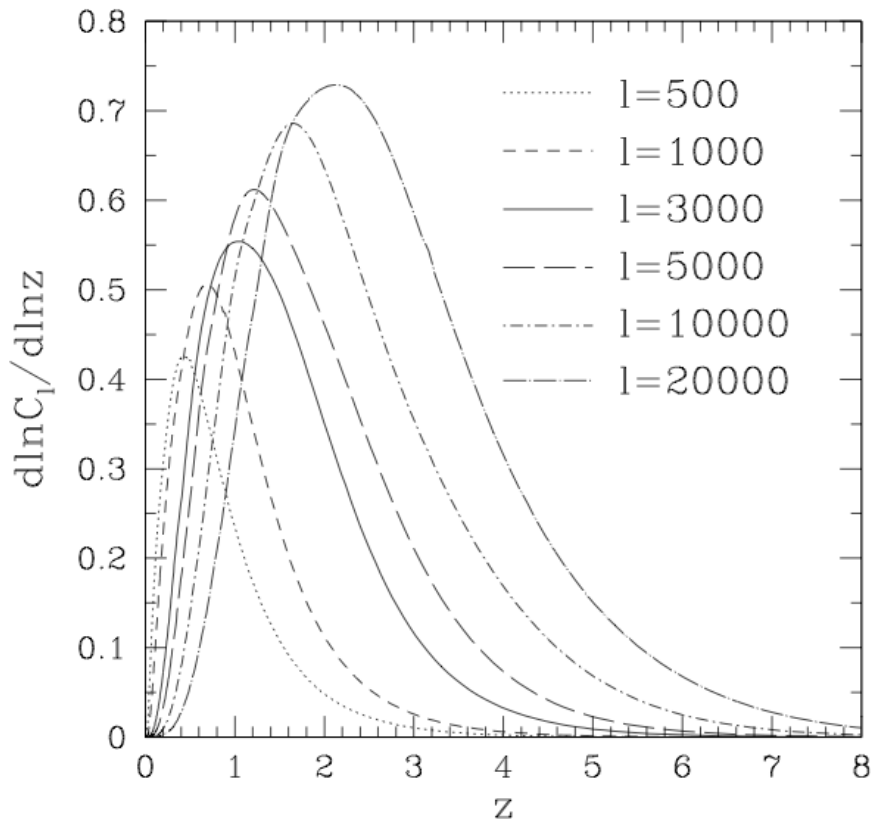
Compares well with Universal Pressure profile and the  $Y-M_{500}$  relns.

Very fast and so can be efficiently used in MCMC (just for SZ CI

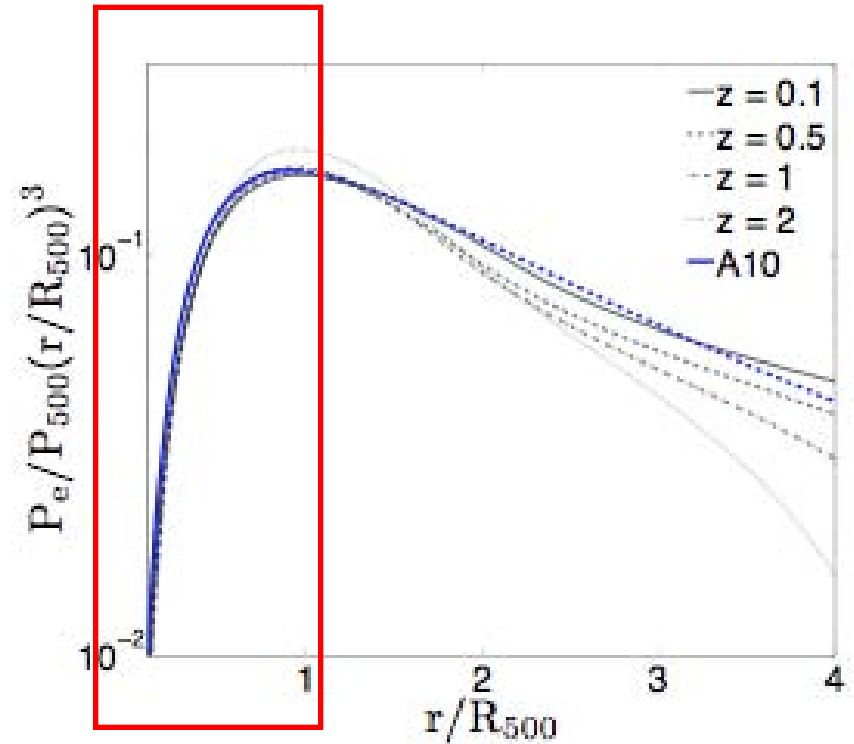
or jointly with Xray scaling observations!)

Chaudhuri & SM, 2010

# SZ Cls - Importance of understanding evolution of pressure profile at high-z



Komatsu & Seljak 2003



Shaw et al 2010

# ICM Entropy ...

Entropy is fundamental because-

- 1) determines structure of the ICM
- 2) record the thermodynamic history of ICM.

Entropy distribution and DM potential completely determines the Xray properties of a relaxed cluster

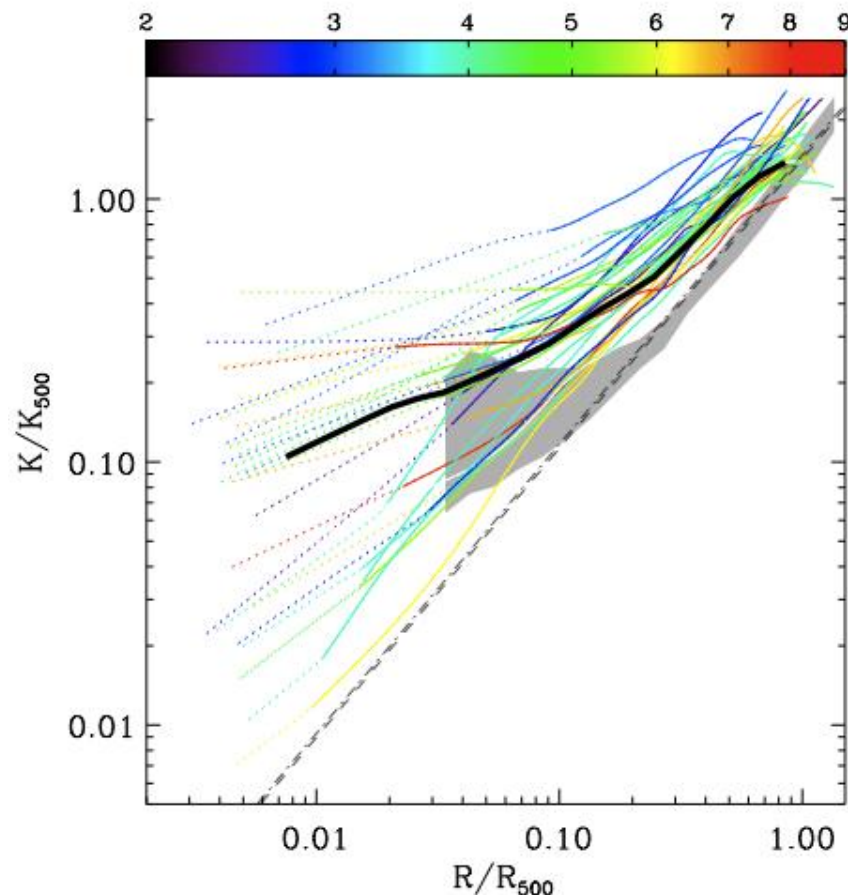
The gas density and temperature profiles in this state of equilibrium are just manifestations of its entropy distribution.

From Voit 2005

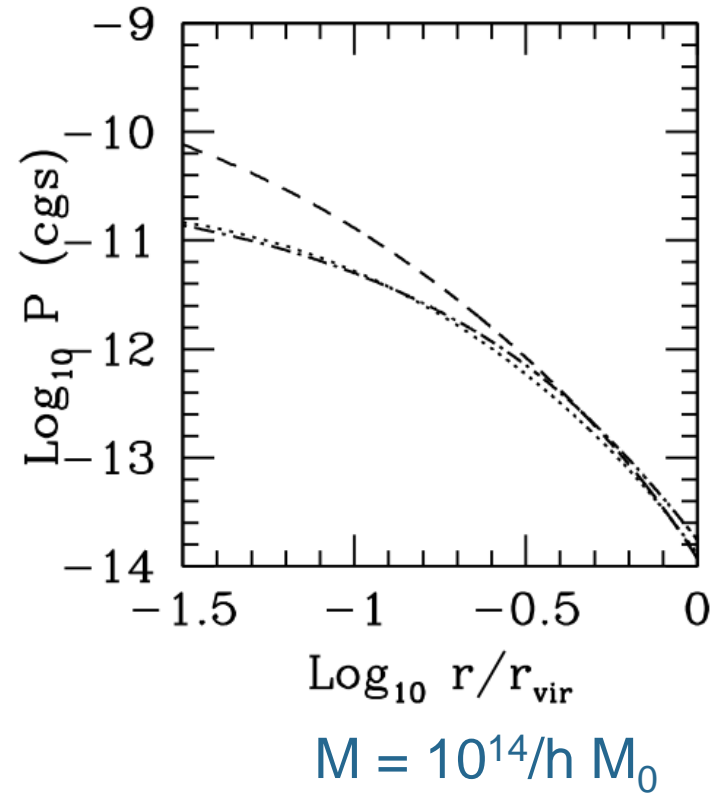
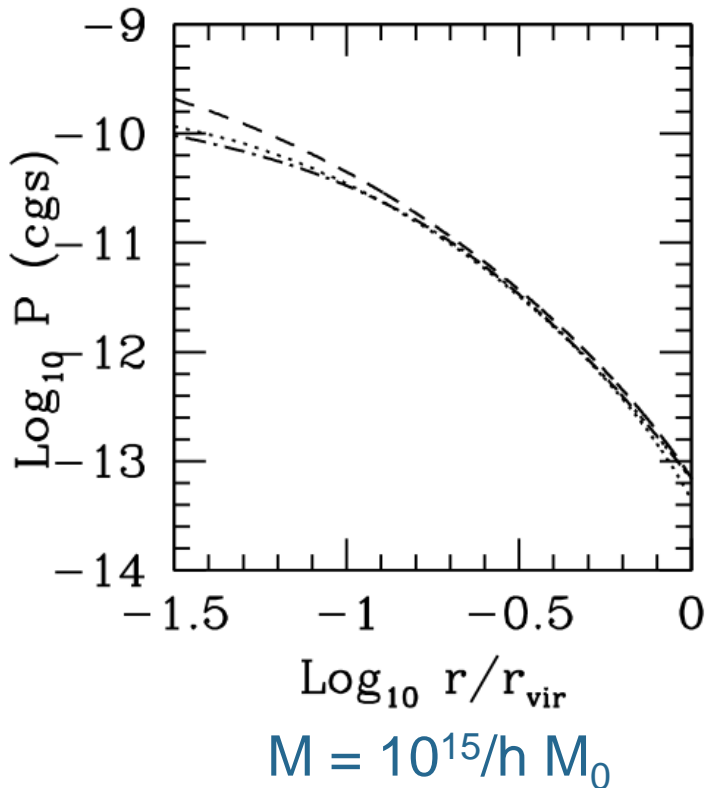
For clusters, Entropy:  $S = k_B T n_e^{-2/3}$

Entropy gives us an idea of the energy/particle in ICM

Pratt etal 2010



## The prescription -



## A “Universal” Entropy *Injection* Prescription

$$S_{inj}(F_g) = 200 \text{ keV cm}^{-2} + 2 \times \left( \frac{M_{\text{vir}}}{10^{14} h^{-1} M_{\odot}} \right)^{-0.2} \times S_i(F_g)$$

Nath & SM 2011

$z = 0$ , for  $10^{14} \leq M_{\text{vir}}/M_{\odot} \leq 10^{15}$

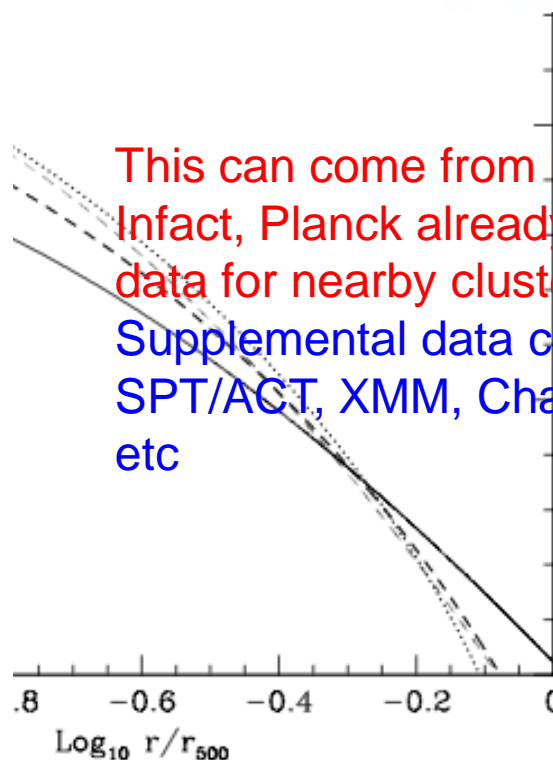
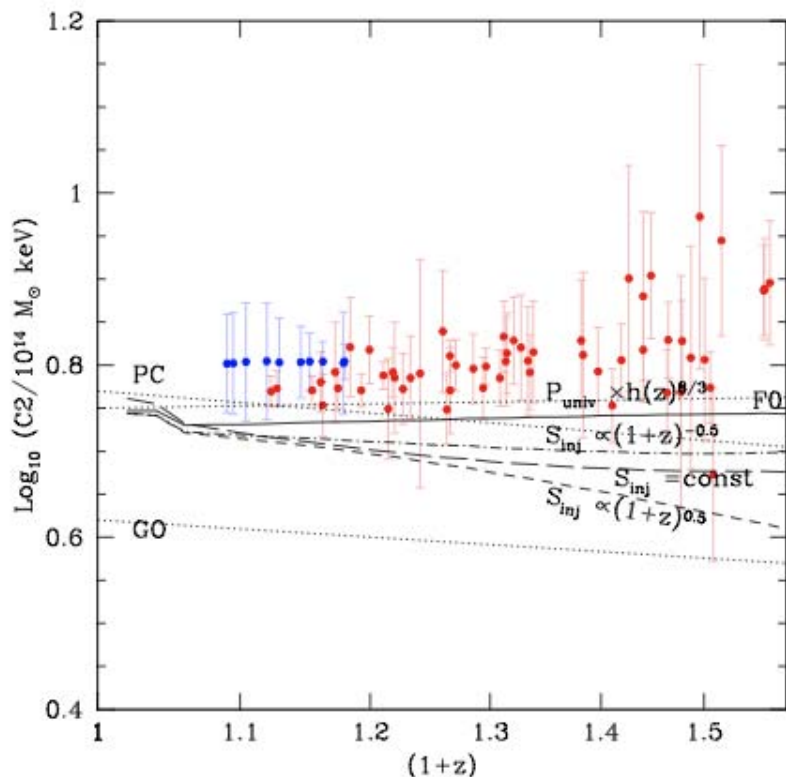
# The Redshift Evolution of Entropy Injection

## Prescription

$$S_{inj}(z) = (1+z)^\alpha S_{inj,z=0}$$

Look at this scaling:

$$Y_X E(z)^{-2/3} = C2 \left( \frac{M_{500}}{5 \times 10^{14} h^{-1} M_\odot} \right)^\alpha$$



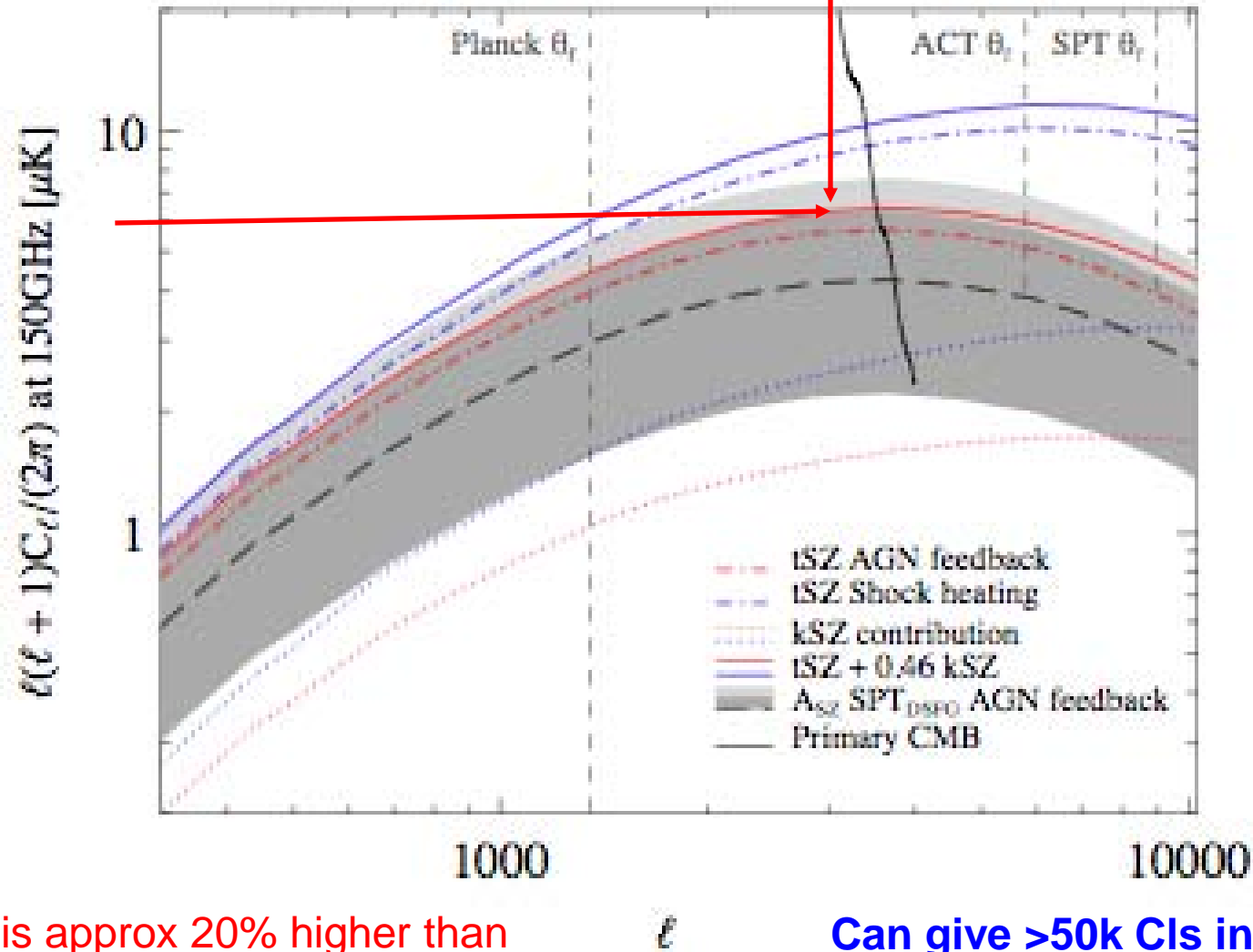
This can come from Planck data. Infact, Planck already has the first data for nearby clusters.

Supplemental data can come from SPT/ACT, XMM, Chandra, eROSITA etc

Atleast  $S_{inj} \propto E(z)^{-2/3} (1+z)^{0.6}$

Needs more evolution than 'self-similar' scaling. At least  $S_{inj} > (1+z)^{-1}$ , i.e.,

# Finally, the SZ CI...



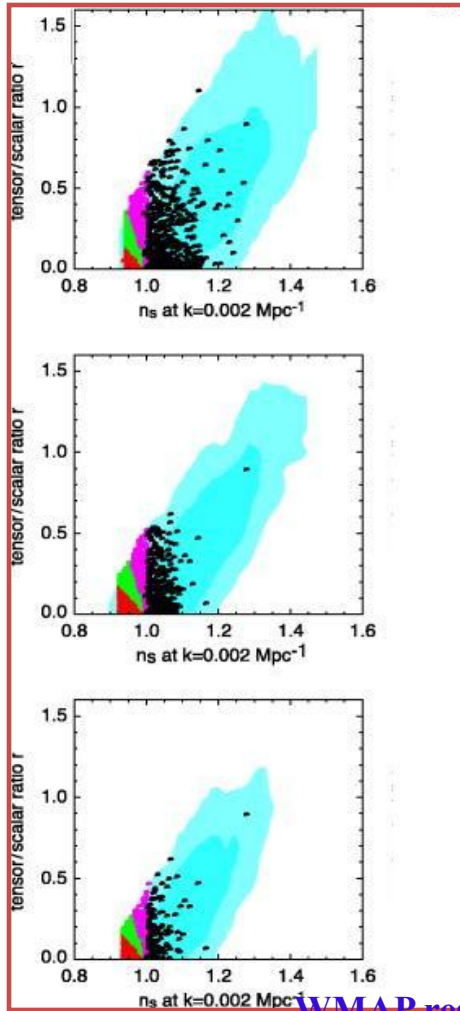
SZ CI is approx 20% higher than Battaglia et al.

Can give >50k CIs in the same time

varying cosmo and gas physics.

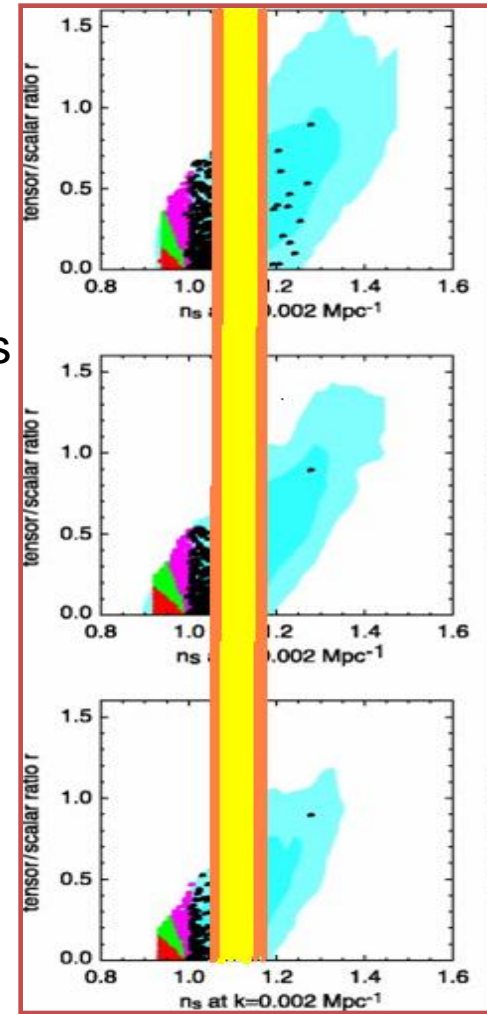
# Constraining inflationary models:

CMB



WMAP results from  
Peiris et al 2004

CMB  
+  
Clusters



# Summary ...

Planck is the first full sky SZ experiment. It will provide us with full sky SZ cluster catalogs and SZ diffuse maps for power spectrum.

The cluster numbers are small that past expectations (many reasons). However, clusters alone can give competitive constraints on  $\Omega_M$  and  $\sigma_8$  compared to CMB anisotropies in Planck.  
Needs extra info to give constraints on 'w'

Combined with Xray surveys, Planck clusters can trace out  $dA(z)$ .

Planck clusters serve as very good calibration sample for -

- 1) Other  $dA(z)$  with clusters
- 2) Model calibrations for gas pressure profile and SZ Cl.

**THANKS...**



**Indo-UK Scientific Seminar:  
Confronting particle-cosmology with Planck & LHC  
IUCAA: 10-12 Aug, 2011**